

Correction 1

a. $\frac{2}{7} + \frac{3}{11} = \frac{22}{77} + \frac{21}{77} = \frac{22+21}{77} = \frac{43}{77}$

b. $\frac{5}{8} + 2 = \frac{5}{8} + \frac{16}{8} = \frac{5+16}{8} = \frac{21}{8}$

c. $\frac{16}{3} - \frac{24}{6} = \frac{32}{6} - \frac{24}{6} = \frac{32-24}{6} = \frac{8}{6} = \frac{4 \times 2}{3 \times 2} = \frac{4}{3}$

d. $\frac{-2}{4} + \frac{5}{6} = \frac{-6}{12} + \frac{10}{12} = \frac{-6+10}{12} = \frac{4}{12} = \frac{4}{4 \times 3} = \frac{1}{3}$

e. $-\frac{3}{11} + \frac{-4}{5} = -\frac{15}{55} + \frac{-44}{55} = \frac{-15-44}{55} = \frac{-59}{55} = -\frac{59}{55}$

f. $\frac{2}{4} + \frac{2}{-4} = \frac{2}{4} + \frac{-2}{4} = \frac{2-2}{4} = 0$

g. $\frac{6}{8} - \frac{-2}{6} = \frac{18}{24} - \frac{-8}{24} = \frac{18 - (-8)}{24} = \frac{18+8}{24} = \frac{26}{24} = \frac{13 \times 2}{12 \times 2} = \frac{13}{12}$

h. $-\frac{5}{12} - \frac{-2}{3} = \frac{-5}{12} + \frac{2}{3} = \frac{-5}{12} + \frac{8}{12} = \frac{-5+8}{12} = \frac{3}{12} = \frac{3}{3 \times 4} = \frac{1}{4}$

i. $2 + \frac{-3}{2} = \frac{4}{2} + \frac{-3}{2} = \frac{4-3}{2} = \frac{1}{2}$

Correction 2

a. $-\frac{1}{6} + \frac{1}{-4} = \frac{-1}{6} + \frac{-1}{4} = \frac{-2}{12} + \frac{-3}{12} = \frac{-2-3}{12} = \frac{-5}{12} = -\frac{5}{12}$

b. $\frac{5}{14} - \frac{3}{4} = \frac{10}{28} - \frac{21}{28} = \frac{10-21}{28} = \frac{-11}{28} = -\frac{11}{28}$

c. $\frac{-3}{15} - \frac{-4}{25} = \frac{-3}{5 \times 3} - \frac{-4}{25} = \frac{-1}{5} + \frac{4}{25} = \frac{-5}{25} + \frac{4}{25} = \frac{-5+4}{25} = \frac{-1}{25}$

d. $-\frac{1}{3} + \frac{5}{2} - \frac{5}{4} = \frac{-4}{12} + \frac{30}{12} - \frac{15}{12} = \frac{-4+30-15}{12} = \frac{11}{12}$

Correction 3

a. $\frac{5}{-3} \times \frac{-4}{7}$ est positif;

b. $\frac{12}{-5} \times \frac{-4}{-3}$ est négatif;

c. $-\frac{5}{-14} \times \frac{-4}{15}$ est négatif;

d. $-\frac{11}{-5} \times \frac{-10}{11}$ est négatif;

e. $\frac{7}{-6} \times \left(-\frac{36}{-17}\right)$ est négatif;

f. $- \left(-\frac{9}{-7}\right) \times \left(-\frac{25}{27}\right)$ est positif.

Correction 4

a. $\frac{3 \times 2 \times 5}{2 \times 5 \times 7} = \frac{3 \times \cancel{2} \times \cancel{5}}{\cancel{2} \times \cancel{5} \times 7} = \frac{3}{7}$

b. $\frac{5 \times 12 \times 7}{7 \times 12 \times 3} = \frac{5 \times \cancel{12} \times \cancel{7}}{\cancel{7} \times \cancel{12} \times 3} = \frac{5}{3}$

c. $\frac{3 \times 4}{4 \times 5 \times 3} = \frac{\cancel{3} \times \cancel{4}}{\cancel{4} \times 5 \times \cancel{3}} = \frac{1}{5}$

d. $\frac{12 \times 5}{4 \times 7} = \frac{3 \times 4 \times 5}{4 \times 7} = \frac{3 \times \cancel{4} \times 5}{\cancel{4} \times 7} = \frac{15}{7}$

e. $\frac{15 \times 11}{3 \times 4} = \frac{3 \times 5 \times 11}{3 \times 4} = \frac{\cancel{3} \times 5 \times 11}{\cancel{3} \times 4} = \frac{55}{4}$

f. $\frac{7 \times 3}{12 \times 5} = \frac{7 \times 3}{3 \times 4 \times 5} = \frac{7 \times \cancel{3}}{\cancel{3} \times 4 \times 5} = \frac{7}{20}$

Correction 5

a. $\frac{9}{7} \times \frac{14}{15} = \frac{9}{\cancel{7}} \times \frac{\cancel{7} \times 2}{15} = \frac{3 \times \cancel{3}}{1} \times \frac{2}{\cancel{3} \times 5} = \frac{3}{1} \times \frac{2}{5} = \frac{6}{5}$

b. $\frac{7}{8} \times \frac{3}{14} \times \frac{4}{9} = \frac{\cancel{7}}{4 \times 2} \times \frac{\cancel{3}}{\cancel{7} \times 2} \times \frac{\cancel{4}}{3 \times \cancel{3}} = \frac{1}{2 \times 2 \times 3} = \frac{1}{12}$

c. $\frac{17}{81} \times \frac{9}{8} \times \frac{7}{34} \times \frac{64}{70} = \frac{17}{\cancel{9} \times 9} \times \frac{\cancel{9}}{8} \times \frac{\cancel{7}}{17 \times 2} \times \frac{8 \times 8}{\cancel{7} \times 10} = \frac{8}{9 \times 2 \times 10} = \frac{2 \times \cancel{2} \times \cancel{2}}{9 \times \cancel{2} \times \cancel{2} \times 5} = \frac{2}{45}$

Correction 6

a. $\frac{5 \times 21}{14 \times 20} = \frac{\cancel{5} \times \cancel{7} \times 3}{\cancel{7} \times 2 \times \cancel{5} \times 4} = \frac{3}{2 \times 4} = \frac{3}{8}$

b. $\frac{15 \times 12}{9 \times 25} = \frac{\cancel{5} \times \cancel{3} \times 4 \times \cancel{3}}{\cancel{3} \times \cancel{3} \times 5 \times \cancel{5}} = \frac{4}{5}$

c. $\frac{24 \times 28}{18 \times 7} = \frac{\cancel{6} \times 4 \times \cancel{7} \times 4}{\cancel{6} \times 3 \times \cancel{7}} = \frac{16}{3}$

d. $\frac{99 \times 25}{22 \times 125} = \frac{\cancel{11} \times 9 \times \cancel{25}}{\cancel{11} \times 2 \times \cancel{25} \times 5} = \frac{9}{2 \times 5} = \frac{9}{10}$

e. $\frac{9 \times 12 \times 10}{27 \times 10 \times 6} = \frac{9 \times 6 \times 2 \times 1}{9 \times 3 \times 1 \times 6} = \frac{\cancel{9} \times \cancel{6} \times 2}{\cancel{9} \times 3 \times \cancel{6}} = \frac{2}{3}$

f. $\frac{3 \times 6 \times 8}{16 \times 12 \times 18} = \frac{\cancel{3} \times \cancel{6} \times \cancel{8}}{\cancel{8} \times 2 \times \cancel{12} \times \cancel{18}} = \frac{1}{24}$

Correction 7

a. $1 + \frac{1}{-2} \times \frac{1}{2} = 1 + \frac{1}{-4} = 1 - \frac{1}{4} = \frac{4}{4} - \frac{1}{4} = \frac{3}{4}$

b. $\frac{5}{9} \times \frac{27}{4} + \frac{5}{6} = \frac{5 \times \cancel{9} \times 3}{\cancel{9} \times 4} + \frac{5}{6} = \frac{5 \times 3}{1 \times 4} + \frac{5}{6} = \frac{15}{4} + \frac{5}{6} = \frac{45}{12} + \frac{10}{12} = \frac{45+10}{12} = \frac{55}{12}$

c. $\frac{3}{7} + \frac{8}{4} \times \left(-\frac{1}{2}\right) = \frac{3}{7} - \frac{8}{8} = \frac{3}{7} - 1 = \frac{3}{7} - \frac{7}{7} = \frac{3-7}{7} = \frac{-4}{7} = -\frac{4}{7}$

d. $\frac{-7}{15} \times \frac{-5}{21} - \frac{-4}{3} = \frac{7}{15} \times \frac{5}{21} + \frac{4}{3} = \frac{\cancel{7} \times \cancel{5}}{\cancel{5} \times 3 \times \cancel{7} \times 3} + \frac{4}{3} = \frac{1 \times 1}{1 \times 3 \times 1 \times 1} + \frac{4}{3} = \frac{1}{9} + \frac{4}{3} = \frac{1}{9} + \frac{12}{9} = \frac{13}{9}$

e. $-3 + \frac{9}{5} \times 3 = \frac{-15}{5} + \frac{27}{5} = \frac{-15+27}{5} = \frac{12}{5}$

f. $\left(\frac{3}{15} - \frac{3}{20}\right) \times \frac{5}{9} = \left(\frac{1}{5} - \frac{3}{20}\right) \times \frac{5}{9} = \left(\frac{4}{20} - \frac{3}{20}\right) \times \frac{5}{9} = \frac{1}{20} \times \frac{5}{9} = \frac{1 \times \cancel{5}}{\cancel{5} \times 4 \times 9} = \frac{1 \times 1}{1 \times 4 \times 9} = \frac{1}{36}$

Correction 8

$$\text{a. } \frac{8}{3} \div \frac{12}{3} = \frac{\cancel{4} \times 2}{\cancel{3}} \times \frac{\cancel{3}}{\cancel{4} \times 3} = \frac{2 \times 1}{1 \times 3} = \frac{2}{3}$$

$$\text{b. } \frac{18}{3} \div 9 = \frac{\cancel{9} \times 2}{\cancel{3}} \times \frac{1}{\cancel{9}} = \frac{2}{3}$$

$$\text{c. } \frac{3}{\frac{4}{6}} = 3 \times \frac{3 \times \cancel{2}}{2 \times \cancel{2}} = 3 \times \frac{3}{2} = \frac{9}{2}$$

$$\text{d. } \frac{\frac{4}{12}}{\frac{20}{3}} = \frac{4}{12} \times \frac{3}{20} = \frac{\cancel{4}}{\cancel{4} \times 3} \times \frac{\cancel{3}}{5 \times \cancel{4}} = \frac{1 \times 1}{4 \times 5} = \frac{1}{20}$$

$$\text{e. } \frac{\frac{14}{26}}{\frac{28}{39}} = \frac{14}{26} \times \frac{39}{28} = \frac{\cancel{14}}{\cancel{13} \times 2} \times \frac{\cancel{13} \times 3}{\cancel{14} \times 2} = \frac{1}{2} \times \frac{3}{2} = \frac{3}{4}$$

$$\text{f. } \frac{\frac{25}{16}}{\frac{15}{15}} = \frac{25}{16} \times \frac{1}{15} = \frac{\cancel{5} \times 5}{16} \times \frac{1}{\cancel{5} \times 3} = \frac{5}{16} \times \frac{1}{3} = \frac{5}{48}$$

Correction 9

1. ● Le calcul **A** donne pour résultat $\frac{1}{3}$.

● Le calcul **B** donne pour résultat $\frac{5}{12}$.

2. Voici les deux expressions symbolisant ces deux calculs :

● Pour le calcul **A** : $\frac{\frac{4}{5} - \frac{2}{3}}{\frac{2}{5}}$

● Pour le calcul **B** : $\left(\frac{\frac{1}{3}}{\frac{2}{7}} - 1 \right) \times \frac{5}{2}$

Correction 10

$$\begin{aligned} \text{a. } -3 \times \frac{\frac{5}{4}}{\frac{15}{6}} + \frac{5}{\frac{1}{2}} &= -3 \times \frac{5}{4} \times \frac{6}{15} + 5 \times \frac{2}{1} - 3 \times \frac{\overset{1}{\cancel{5}}}{\underset{2}{\cancel{4}}} \times \frac{\overset{3}{\cancel{6}}}{\underset{3}{\cancel{15}}} + 10 \\ &= -3 \times \frac{1}{2} \times \frac{3}{3} + 10 = \frac{-3}{2} + 10 = \frac{-3}{2} + \frac{20}{2} \\ &= \frac{-3 + 20}{2} = \frac{17}{2} \end{aligned}$$

$$\begin{aligned} \text{b. } \frac{3 + \frac{2}{5}}{3 - \frac{10}{10}} &= \frac{\frac{15}{5} + \frac{2}{5}}{\frac{30}{10} - \frac{10}{10}} = \frac{\frac{15+2}{5}}{\frac{30-10}{10}} = \frac{\frac{17}{5}}{\frac{20}{10}} = \frac{17}{5} \times \frac{10}{20} \\ &= \frac{17}{\cancel{5}} \times \frac{\cancel{5} \times 2}{26} = \frac{17}{1} \times \frac{2}{26} = \frac{17}{1} \times \frac{\cancel{2}}{\cancel{2} \times 13} = \frac{17}{1} \times \frac{1}{13} = \frac{17}{13} \end{aligned}$$

$$\begin{aligned} \text{c. } \frac{\frac{3}{5} - \frac{15}{12} \times \frac{6}{33}}{\frac{66}{12} + \frac{4}{33}} &= \frac{\frac{3}{5} - \frac{\cancel{3} \times 5}{\cancel{2} \times 4} \times \frac{\cancel{2} \times 3}{\cancel{3} \times 9}}{\frac{11 \times 6}{4 \times 3} \times \frac{4}{11 \times 3}} = \frac{\frac{3}{5} - \frac{5}{4} \times \frac{3}{9}}{\frac{6}{3} + \frac{4}{3}} \\ &= \frac{\frac{3}{5} - \frac{5}{4} \times \frac{1}{3}}{\frac{6}{12} + \frac{1}{3} \times \frac{1}{3}} = \frac{\frac{3}{5} - \frac{5}{12}}{\frac{6}{12} + \frac{4}{12}} = \frac{\frac{18}{60} - \frac{25}{60}}{\frac{10}{12} + \frac{4}{12}} \\ &= \frac{\frac{18-25}{60}}{\frac{14}{12}} = \frac{\frac{-7}{60}}{\frac{7}{3}} = \frac{-7}{60} \times \frac{3}{7} = -\frac{1}{20} \end{aligned}$$